## Sampling in Geometric Set Systems

Homework 4

Suppose that for any integer $k$ there is a set $P_{k}$ of $\Omega(k \log k)$ points in $\mathbb{R}^{2}$ such that for any $Q \subset P_{k}$ there are $k$ lines that cover $Q$ but are disjoint from $P_{k} \backslash Q$. Prove that any $\varepsilon$-net for the set system induced by lines in the plane has size $\Omega(1 / \varepsilon \log (1 / \varepsilon))$.

